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4	Probabilistic rejection templates in visual working memory
5	Andrey Chetverikov ^{a,b,c} , Gianluca Campana ^{d,e} , & Árni Kristjansson ^{b,f}
6	^a - Center for Cognitive Neuroimaging, Donders Institute for Brain, Cognition and Behavior,
7	Radboud University; ^b - Laboratory for Visual Perception and Visuomotor Control, Faculty of
8	Psychology, School of Health Sciences, University of Iceland, Reykjavik, Iceland; ^c - Cognitive
9	Research Lab, Russian Academy of National Economy and Public Administration, Moscow,
10	Russia; ^d – Department of General Psychology, University of Padova, Padova, Italy; ^e - Human
11	Inspired Technology Research Centre, University of Padova, Italy; ^f - School of Psychology,
12	National Research University Higher School of economics.
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15	Author Note
16	Correspondence should be addressed to: Andrey Chetverikov, Donders Institute for Brain,
17	Cognition and Behavior, Center for Cognitive Neuroimaging, Kapittelweg 29, 6525 EN
18	Nijmegen, The Netherlands. Email: <u>a.chetverikov@donders.ru.nl</u> . The preprint of this paper is
19	available at https://dx.doi.org/10.17605/OSF.IO/VRBGH The data from the experiments
20	reported in this paper and scripts for simulations and analyses are available at <u>https://osf.io/rg2h8</u>
21	Word count: 4740.

Abstract

23 Our interactions with the visual world are guided by attention and visual working memory. 24 Things that we look for and those we ignore are stored as templates that reflect our goals and the 25 tasks at hand. The nature of such templates has been widely debated. A recent proposal is that 26 these templates can most straightforwardly be thought of as probabilistic representations of task-27 relevant features. We assessed observers' representations by measuring the slowing of visual 28 search when distractor templates unexpectedly match the target. To provide a strong test of the 29 templates' probabilistic nature, distractor stimuli were heterogeneous, randomly drawn on each 30 trial from a bimodal probability distribution. Using two targets on each trial, we tested whether 31 observers encode the full distribution, only one peak of it, or the average of the two peaks. 32 Search was slower when the two targets corresponded to the two modes of previous distractor 33 distributions than when one target was at one of the modes and another between the modes or 34 outside the distribution range. Furthermore, targets on the modes were reported later than targets 35 between the modes that, in turn, were reported later than targets outside this range. These results 36 show that observers represent both distribution modes using templates based on the full 37 probability distribution rather than single features or simple summary statistics. Our findings 38 indicate that visual working memory templates guiding attention are probabilistic and 39 dynamically adapt to task requirements, reflecting the probabilistic nature of the input.

Keywords: attentional templates, visual working memory, probabilistic representations, visual
ensembles, summary statistics, visual search.

Probabilistic rejection templates in visual working memory

45 Our senses are constantly bombarded with an overwhelming amount of information that needs to 46 be filtered by the brain to guide action. This information, however, is not completely chaotic. For 47 example, leaves on a tree usually have similar colors, and colors within a single leaf would be 48 more similar to each other than to another leaf. Probabilistic models of vision (Bejjanki, Beck, 49 Lu, & Pouget, 2011; Feldman, 2014; Girshick, Landy, & Simoncelli, 2011; Kersten, Mamassian, 50 & Yuille, 2004; Ma, 2012; Rao, Olshausen, & Lewicki, 2002) suggest that the brain utilizes 51 existing correlations in the environment and uses them in perception. However, some of the 52 incoming information is not relevant for current behavior, and it is important to reject it while 53 processing other stimuli in more detail. Traditionally, the rejection of irrelevant information 54 within a specific feature dimension (e.g., orientation) is thought to be based on specific feature 55 values (Woodman, Carlisle, & Reinhart, 2013). Here we ask whether such rejection can instead 56 be based on probabilistic templates. If this is the case, then probabilistic inference in the brain 57 does not start with perception, but sooner, when to-be-rejected templates are formed (based on previously encountered stimuli) to optimize the prioritization of what is perceived. 58

59 Imagine a radiologist looking for signs of tumor in x-ray scans. Malignant signs can take 60 many forms so the targets to look for are diverse. By many accounts, search in this and other 61 contexts is thought to be guided by templates held in visual working memory (Woodman et al., 62 2013). These templates reflect what one should look for, but may also reflect what should be 63 ignored (Arita, Carlisle, & Woodman, 2012; Won & Geng, 2018). For example, distractors such 64 as the rib cage on a lung scan are salient but not informative and radiologists can therefore ignore it. It is well known that the information about to-be-ignored stimuli or features is kept in 65 66 memory, but the way they are represented is still unknown.

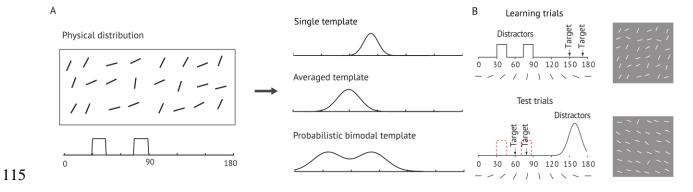
67 There are capacity limits in the amount of information that can be stored in visual working memory templates (Bundesen, 1990; Grubert & Eimer, 2013; Vickery, King, & Jiang, 68 69 2005), with some authors even suggesting that only one template containing a single feature 70 value can guide attention at any given time (Oberauer, 2002; Olivers, Peters, Houtkamp, & 71 Roelfsema, 2011; van Moorselaar, Theeuwes, & Olivers, 2014). Alternatively, templates could 72 be conceptualized as probabilistic entities of varying precision (Bays, 2015) rather than matches 73 to exact feature values. While previous studies found some support for this, observers typically 74 reported features of single items (Ma, Husain, & Bays, 2014). However, in the real world such 75 isolated features practically never occur. Furthermore, with a few exceptions (Arita et al., 2012; Won & Geng, 2018), templates for ignored information are rarely studied. Here, we provide 76 77 strong evidence for the probabilistic template view by testing visual working memory templates 78 for rejection.

79 Our observers searched for two oddly oriented targets among distractors randomly drawn 80 from a bimodal orientation distribution. To expose observers' templates, after a sequence of 81 *learning* trials with distractors randomly drawn from a bimodal distribution, targets on *test* trials 82 could either correspond to regions of feature space previously used for distractors, fall in 83 between the modes of the bimodal distribution, or have feature values outside the previous 84 distribution range. We assume that observers' templates reflect what has been relevant on recent 85 trials. If templates contain features of distractors to be ignored, which then become targets on test 86 trials, search should be slower than otherwise (Chetverikov, Campana, & Kristjánsson, 2016; 87 Kristjánsson & Driver, 2008; Lamy, Antebi, Aviani, & Carmel, 2008; Maljkovic & Nakayama, 88 1994; Wang, Kristjánsson, & Nakayama, 2005). Crucially, experiments with varied set size and trial numbers show that learning in this paradigm cannot be explained by the sampling of a few 89

90 items (Chetverikov, Campana, & Kristjánsson, 2017d, 2017b). It also cannot be explained by 91 simple decision rule learning (e.g., all stimuli that have features in a certain range are 92 distractors), because observers response times, on average, reflect the shape of the distractor 93 distribution rather than just a boundary between a target and distractors (Chetverikov et al., 2016, 2017b; Chetverikov, Campana, & Kristjánsson, 2017c; Chetverikov, Hansmann-Roth, Tanrikulu, 94 95 & Kristjansson, 2019). However, it is not yet clear whether each single set of learning trials can 96 feed observers' templates with the feature probability distribution of distractors, nor is it clear 97 how accurately the information is stored in the templates.

98 Under the *strong* probabilistic template hypothesis, templates would include information 99 about both peaks of a bimodal distribution. That is, the template would accurately reflect the information about the full probability distribution. Alternatively, templates might include only a 100 101 single peak (e.g., the attended one), or might reflect only the summary statistics, such as the 102 averages of the whole distribution (Alvarez, 2011). With a two-target search we were able to test 103 whether observers encode both peaks of a distribution following a single learning sequence. The 104 predictions of these models (see Simulations) are qualitatively different regarding both the order 105 in which targets are reported in a two-target search, and search times. If observers accurately 106 encode a bimodal distribution, on trials with a target on a peak and target between peaks, targets 107 between the peaks (associated with a lower distractor probability) should be reported before 108 targets on peaks (associated with the highest distractor probability, Figure 1A). In contrast, if 109 only one peak is encoded or if the whole distribution is averaged, targets on peaks would be 110 associated with a lower distractor probability and should be reported no later than targets 111 between the peaks (associated with lower distractor probability in this case). Notably, while all 112 three hypotheses postulate that observers can use probabilistic inference, only the first one

- 113 assumes that the distractor probability distribution is encoded accurately, that is, that the
- 114 observers use relatively accurate probabilistic *templates*.



- 116 **Figure 1.** Panel A: The same physical bimodal distribution can be represented in different ways. Panel B:
- 117 Example learning and test trials with distractor distributions and targets shown on the left.



Experiment

Ethics Statement. The study was approved by the ethics committee of St. Petersburg
State University (#75, 21.06.2017). All participants signed a consent form before taking part in
the study.

123 **Participants.** Fifteen observers (ten female, age M = 25.67) at St. Petersburg State 124 University, Russia, participated voluntarily in a single experimental session lasting 125 approximately 30 min. The data from two observers were excluded because their response times 126 on test trials were too slow (M = 1464 and M = 1871 ms), compared with other observers (M =127 1064 ms). Following our previous studies (Chetverikov et al., 2016, 2017b, 2017c, 2017d), the 128 design of this study utilized within-subject comparisons with a relatively small number of trained 129 observers (each observer was trained for at least 100 trials before the main session) performing a 130 large number of trials. The sample size and the trial numbers were similar to those in previous 131 studies using the same paradigm. 132 Method. We used a task similar to our previous studies (Chetverikov et al., 2016, 133 2017b). Stimuli were presented on an Acer V193 display (19" with 1280×1024 pixel resolution) 134 using PsychoPy 1.84.2 (Peirce, 2007, 2009). Viewing distance was ~ 60 cm. Observers searched for two oddly oriented lines in a 6×6 grid of 36 lines subtending $16^{\circ} \times 16^{\circ}$ at the centre of a 135 136 display. The length of each line was 1.41°. Line positions were jittered by randomly adding a value between $\pm 0.5^{\circ}$ to both vertical and horizontal coordinates. 137 138 Observers were instructed to search for two targets on each trial, with targets being the 139 stimuli that were most different from all the others ("odd-one-out" search (Maljkovic & 140 Nakayama, 1994)). Targets were randomly distributed between the four quadrants of the search

display with the constraint that the two targets on a given trial could not appear in the same quadrant. Observers reported the locations of the targets by pressing one of four keys ('f', 'g', 'r', 't' on a standard keyboard) corresponding to the quadrants of the search display. They were informed that two targets would be presented on each trial and were encouraged to respond to each target as soon as they found it and not wait until both targets were found.

146 Trials were organized in intertwined prime and test 'streaks'. During prime streaks, 147 distractors were randomly drawn from a bimodal distribution that included two uniform parts 148 with orientations ranging from -30 to -20 and +20 to +30 relative to the overall mean. The 149 distribution mean was the same within streak but chosen randomly between streaks. Target 150 orientations were selected randomly on each trial with the restriction that the distance between 151 target orientation and distractor mean in feature space was 60 degrees at minimum. Prime streak 152 length was set to 6-7 trials (with equal probability) because this streak length is sufficient to learn 153 bimodal distributions with relative accuracy (Chetverikov et al., 2017b). 154 Within test streaks, distractor orientations were randomly drawn from a truncated 155 Gaussian with SD = 10 deg. and range 20 deg. Test streaks had one or two trials (with equal 156 probability). Different *target* types were used on test trials: targets were either located on a peak 157 of the previous bimodal distribution ("Peak", at +/-25 deg. relative to the previous distractor 158 mean), between the peaks ("Between", at 0 deg.) or outside the previous distribution range 159 ("Outside", at +/-50 deg.). Four types of test streaks were used: 1) with two targets either on two 160 different peaks ("Peak + Peak"); 2) on a peak and in-between the peaks ("Peak + Between"); 3) 161 on a peak and outside the previous distribution range ("Peak + Outside" – where the "outside" 162 target was always 25 deg. away from the target peak, that is, either the two targets were oriented

163 at +25 and +50 deg. or -25 and -50 relative to the previous distractors' mean); 4) between the

peaks and outside the range ("Outside + Between"). These four *test types* were presented equally often (40 repetitions by participant) in random order. The distractor mean was chosen to be equidistant from both test targets. The second test trial is not analyzed here as the priming effects from the learning streak are not likely to be significant after the first two-target test search. Twotrial test streaks were added for consistency with previous studies and in order to reduce the potential effects of observers' expectations regarding streak lengths.

Observers participated in one session of approximately 1300 trials. Decision time was not
limited but participants were encouraged to respond as quickly and accurately as possible.

172 Feedback based on search time and accuracy on previous trials was shown in the upper-left

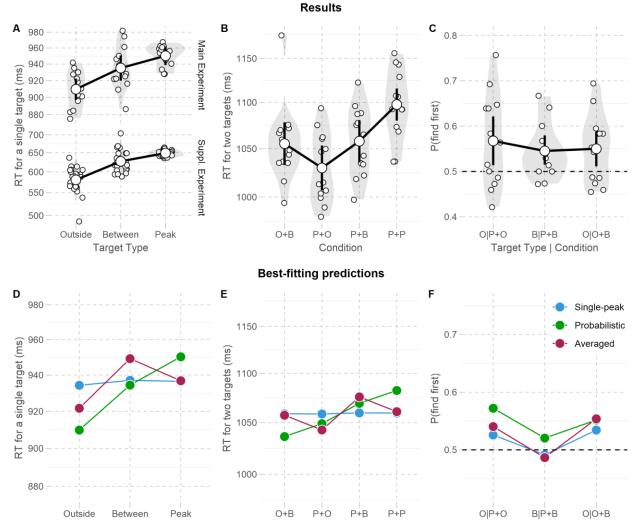
173 corner of the screen to motivate participants (see Chetverikov et al., 2016, for details on feedback

score calculation). The current trial number and the total number of trials were shown beneath

the score. If observers made an error, the word "ERROR" appeared in red letters at display centre

176 for 1 second.

In addition to this two-target search experiment, we also ran a single-target search study
(see Supplementary Experiment). The latter was used as a comparison for the single-target
search time analyses to ensure that the introduction of a second target and specific conditions of
the main experiment did not affect the pattern of results.



182 183 Figure 2. Experimental results and best-fitting predictions of the models (see Simulations). A: Results for 184 different target types from the main Experiment (average search times ignoring the order in which the 185 targets were reported) and the supplementary Experiment where observers searched for only one target on 186 each trial. B: Results for two-target search from the main Experiment. C: Results for the order of target 187 reporting from the main Experiment. D-F: Predictions for single-target search times, search times for two 188 targets, and for the order in which targets would be reported in a two-target search. For A-C large dots 189 show group means, bars show their 95% confidence intervals, smaller dots show individual observers' 190 means, and shaded areas show distributions of individual observers' means. Abbreviations: RT - response 191 times, P - target on a peak, B - target between the peaks, O - target outside the range of previous distractor 192 distribution. The plus sign indicates that two targets of corresponding types are used. For the order of 193 reporting, X|A+B means that target type X was reported first when target types A and B are combined. 194 Note that the slopes of the lines connecting the dots in each plot indicate relative but not absolute 195 difference between conditions because the x-axis is categorical.

197 Results

198 **Overall performance.** On learning trials, observers found both targets in most cases (M 199 = 0.72 [0.67, 0.77]), though the share of trials where only one target was reported was high (M =200 0.27 [0.22, 0.31]; both targets were reported incorrectly on 1% of trials). On test trials, observers 201 reported both targets correctly on M = 0.91 [0.89, 0.93] trials (accuracy was comparable to the 202 results of single-target search in the Supplementary Experiment). The delay between the report 203 on the first and the second target was relatively short, but longer on learning than on test trials 204 (M = 263 [198, 326] vs. M = 176 [130, 233], respectively, t(12.0) = 4.13, p = .001). Similarly, 205 the first target was reported later on learning than test trials (M = 973 [854, 1103] vs. M = 826206 [753, 904], respectively, t(12.0) = 5.23, p < .001).

The learning effects were also comparable to those from the single-target search experiment (see supplement). A linear mixed-effects regression with Helmert contrasts (comparing each trial with the average of the following trials) showed that the first trial was slower, (B = 0.11, SE = 0.01, t(52.57) = 9.61, p < .001) and less accurate (B = -0.04, SE = 0.02, t(13.12) = -2.62, p = .021) than the later trials. The follow-up trials did not differ from one another.

Test trials. Replicating previous results, search times differed depending on target type ($F(2, 24) = 8.28, p = .003, \eta^2_G = .02$, see Figure 2A). Observers search longer for "Peak" targets compared to "Between" targets, which were in turn, found later than "Outside" targets. Crucially, a repeated-measures ANOVA indicated that the time needed to find *both* targets on test trials was affected by the condition ($F(3, 36) = 6.66, p = .002, \eta^2_G = .02$, Figure 2B). Comparisons between conditions with the same feature difference between the targets showed

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that performance on "Peak + Peak" trials was slower than on "Outside + Between" trials ($t(12.0)$
= 3.10, p = .009), while "Peak + Between" trials were not different from "Peak + Outside"
(t(12.0) = -1.68, p = .118) trials. Finally, the "Peak + Peak" condition was also slower than the

222 "Peak + Between" condition (t(12.0) = 2.58, p = .024).

We then analyzed which type of target was reported first in each condition using a 223 224 binomial mixed-effects regression. The results showed that targets on peaks were reported after 225 targets between the peaks (Z = -2.01, p = .044, Figure 2C) or targets outside the preceding 226 distribution range (Z = -2.43, p = .015), while the latter were reported earlier than targets 227 between the peaks (Z = 2.08, p = .037).

In sum, search with two targets on the peaks was the most difficult. A comparison of the 228 229 "Peak + Between" and "Peak + Outside" conditions showed only a numerical difference in total 230 RT. However, in the "Peak + Between" condition, targets on peaks were reported later than 231 targets between the peaks, whereas in the "Outside + Between" condition targets between the 232 peaks were reported later than the "Outside" targets. This shows again that targets on peaks were 233 the most unexpected for observers, followed by targets between the peaks, followed in turn by 234 "Outside" targets that led to the fastest search times.

235 Simulations. We simulated the predictions from three models (Figure 2E-F; the 236 simulation code is available at <u>https://osf.io/rg2h8</u>). For our main model of interest, the 237 "probabilistic" model, we assumed that the probabilities of different distractors can be 238 represented by two Gaussian templates (for simplicity, we ignore the fact that the stimuli 239 distributions might be more accurately represented by non-Gaussian templates (Chetverikov, 240 Campana, & Kristjánsson, 2017a)) centered on the means of distractor distribution segments. We 241 assumed that observers utilize the knowledge they obtained about distractors and targets

(t(12.0))

optimally. According to a Bayesian ideal observer model in a localization search task, to find a target, observers compare the probability that a given noisy measurement of orientation x at each location L is a target versus the probability that it is a distractor (Ma, Navalpakkam, Beck, van den Berg, & Pouget, 2011; Ma, Shen, Dziugaite, & van den Berg, 2015):

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$$p(L|x) \propto p(L) \frac{p(x|T)}{p(x|D)} = p(L) \frac{p(x|s_L)p(s_L|T)ds_L}{p(x|s_L)p(s_L|D)ds_L}$$

where s_L is a true stimulus value at this location, p(L) is the probability that a target is presented at this location, *T* and *D* are the parameters of target and distractor distributions, respectively. In our simulations, we assumed that internal representations of target and distractor distributions are independent and response times are inversely proportional to the amount of evidence p(L/x). Given that all locations in our experiment were equiprobable, that is, p(L) is the same for all locations, response times will, on average, be proportional to the probabilities of the test target θ_T under given distractor template parameters:

254 $RT \propto p(\theta_T | D)$

The width of the Gaussian templates was estimated by fitting the model to single-target response time data. To increase the robustness of the estimates, we used an approach similar to bootstrap aggregating ("bagging"), often employed in machine learning (Breiman, 1996). For each model we obtained 500 bootstrapped samples grouped by participant (that is, on each iteration, sampling with replacement was done for each subject and then the samples were combined). We then estimated the template widths for each sample by fitting response times as a linear function of the stimuli probability. For a probabilistic model:

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$$RT_{1T} = a + b\left(\frac{1}{2}p(\theta_T|\mu_1,\sigma) + \frac{1}{2}p(\theta_T|\mu_2,\sigma)\right)$$

263	where $\mu_1 = 25$ and $\mu_2 = -25$, the means of bimodal distractor distribution peaks, and <i>a</i> and
264	b are the scaling parameters necessary to translate the probabilities into response times. The
265	template widths obtained for each sample were then averaged to get the resulting estimates.
266	Estimated template widths were similar for the experiment reported here (18 deg.) and the
267	supplemental experiment (21 deg.).
268	For the "single-peak" model, we assumed that only one of the two peaks was encoded
269	(with the same approach as with the "probabilistic" model). Given that the peak means are
270	equidistant to the overall distractor mean:
271	$RT_{1T} = a + b(p(\theta_T \mu_1, \sigma))$
272	The estimated template widths were 27 and 22 deg. for the main and the supplemental
273	experiment.
274	Finally, the "averaged" model was based on the idea that observers might use a single set
275	of summary statistics to represent the stimuli. Accordingly, we assumed that observers use a
276	single Gaussian template centered at the mean of the overall bimodal distribution:
277	$RT_{1T} = a + b(p(\theta_T 0,\sigma))$
278	The template width was also obtained using ML optimization and bootstrapping. For the
279	main experiment the estimated width was 114 deg., while for the supplemental experiment it was
280	140 deg. (i.e., almost flat template), already suggesting that this model provides a poor fit to the
281	experimental data.
282	We then used the estimated template widths to obtain the predictions of the three models
283	for the search times for different target types (Figure 2D), total search time for two targets in
284	different conditions (Figure 2E), and for the order in which the targets should be reported (Figure
285	2F). For single-target search the equations were the same as when we estimated the template

286	widths, however, we used the data averaged by target type for each subject to reduce the effect of
287	trial-by-trial variability. Two-target search times were assumed to be proportional to a sum of
288	two search times predicted in the same way as for a single target:
289	$RT_{2T} = a + b(p(\theta_{T1} D) + p(\theta_{T2} D))$
290	where D reflects the distractor distribution parameters for a given model, that is, the
291	template mean(s) and its estimated width(s).
292	Finally, we assumed that all other things being equal, the order in which the targets are
293	reported would depend on the ratio of the probabilities of observing the test targets under the

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$$P(find T2 first) = 0.5 + k \log\left(\frac{p(\theta_{T1}|D)}{p(\theta_{T2}|D)}\right)$$

given distractors template:

with *k* as a scaling constant. The ratio was transformed to logarithm to allow for bothpositive and negative values.

298 Figures 2D and 2E show that the probabilistic model provided more accurate predictions 299 for response times than the other models. For single-target response times, it accurately predicted 300 that targets on peaks would be the hardest to find and targets between the peaks would be harder 301 to find than targets outside the range of previously learned distractors. In contrast, the averaged 302 model (Δ BIC = 5.94; here and later Δ BIC refers to the difference in Bayesian Information 303 Criterion compared to the probabilistic model, positive values meaning that the probabilistic 304 model has better fit) suggested that the targets in-between the peaks would be hardest to find, 305 while the single-peak model ($\Delta BIC = 12.47$) predicted relatively similar response times for 306 between targets and targets on peaks. For two-target RTs, the probabilistic model failed to 307 predict longer search for the "outside + between" condition compared to the "peak + outside" 308 condition. Note, however, that this difference was also not significant in the results of our

309 experiment. Speculatively, it might be a result of a higher similarity between the targets in the 310 latter than in the former. Nevertheless, the predictions of the probabilistic model were still better 311 than of the averaged (Δ BIC = 8.04) or the single-peak model (Δ BIC = 6.59). 312 Crucially, the probabilistic, single-peak, and averaged models gave qualitatively different 313 predictions for the order in which the targets would be found. For both the single-peak and 314 averaged model, the probability of first reporting targets between the peaks when combined with

targets on peaks was below 0.5 (Figure 2C). As outlined in the introduction, when observers

encode only one peak, on 50% of the trials, the "peak" target on test trials should be on this peak

317 while in the other half of the trials in will be on the non-encoded peak. Depending on the width

of the template, the average ratio of the probabilities for a target would vary: with very large or

319 very small template widths, it will be close to 0.5 because targets between the peaks and at the

320 non-encoded peaks will be equally probable, and with intermediate template widths it will be

321 below 0.5 (note that this conclusion is not limited to the specific equation we used for

determining the probability of finding one target before another; in fact, it could be shown that

323 this is the case for any monotonic function describing the transformation of a ratio of

324 probabilities of observing the target under a given Gaussian distractor template into average

325 probability of a given reporting order). For the averaged model the target between the peaks

326 should always be reported later than targets on the peaks. In contrast, for the probabilistic model

327 that accurately encodes the probabilities of distractors, the target between the peaks should be

reported before the target at the peak. Accordingly, the probabilistic model describes the results

better than the single-target ($\Delta BIC = 13.11$) or the averaged model ($\Delta BIC = 6.86$).

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Discussion

332 We assessed the content of templates guiding visual search in the orientation domain, by 333 measuring slowing for targets drawn from a preceding distractor orientation distribution. 334 Crucially, the distribution was bimodal and the searches used to probe the representations 335 involved two simultaneous targets within a trial. Response times were slower when the targets 336 corresponded to the two modes ("peaks") of previous distractor distributions than when one 337 target was from one of the modes and another from between them, while the latter combination 338 of targets resulted in slower search than when one of the targets was outside the previous 339 distractor range. Furthermore, the order in which the targets were reported on a test trial followed 340 the distractor probabilities observed during prime trials. Targets outside the previous distractor 341 range were reported earlier than the ones between the modes, while the latter were reported 342 before the targets at the modes of previous distractor distribution. When we simulated the 343 predictions of probabilistic, single-template, and averaged template models, we found that the 344 probabilistic model predicts the response times pattern for different target types and different 345 conditions far better than the other models. Moreover, only the probabilistic model was able to 346 accurately predict the order in which the targets were reported. Both the single-template model 347 and the averaged-template model predicted that the target between the peaks should on average 348 be reported after the targets at the peaks, while the reverse was accurately predicted by the 349 probabilistic model. The target between the peaks in the "Peak + Between" condition was on 350 average reported before than the target at one of the peaks. This shows that observers 351 simultaneously represent both modes of distractor distributions. Their representations 352 approximate the physical stimuli, and they fill in the gaps in probability space as demonstrated

by slower responses when one of the targets was between the peaks compared to when it wasoutside the previous distractor range.

355 Notably, all three models can be considered probabilistic in a sense that they do provide 356 observers with a measure of probability that a certain feature belongs to a distractor class. The 357 difference is in the degree of simplification. The bimodal model reflects the probability 358 distribution accurately (with the assumption of Gaussian approximation). The two other models 359 taken into consideration, however, diverge from an accurate representation in different ways: the 360 "averaged" assumes the use of overall summary statistics, while the "single-peak" assumes the 361 encoding of only one part of the distribution (which could be caused, for example, by biased 362 sampling). While every heuristic or a decision rule can be cast in term of probabilities (e.g., a 363 delta function that assigns probability of 1 for one part of feature space and 0 for the rest), a 364 probabilistic representation as denoted here provides an accurate representation of the probability 365 distribution of the stimuli.

366 Unlike previous studies assessing how distracting information is stored in visual working 367 memory (Arita et al., 2012; Won & Geng, 2018), the distractors in our studies were 368 heterogeneous and were generated randomly based on a bimodal probability distribution. 369 Nevertheless, observers were able to integrate the information about distractors into an 370 approximate bimodal representation. Speculatively, this demonstrates that using homogeneous 371 distractors may be an artificial limitation, perhaps brought on by earlier technical restrictions on 372 experimental stimuli in pre-modern computer era. In the real world, distracting information is 373 rarely homogeneous, so it may not be particularly surprising that humans are able to form 374 accurate templates representing probability distributions.

375 Following seminal accounts of priming of pop-out effects (Malikovic & Nakayama, 376 1994) we argue that the representations of distractor distributions are kept in visual working 377 memory, rather than long-term memory. Woodman et al. (Woodman et al., 2013) have 378 demonstrated that the representation of a single attended target is transferred from VWM to long-379 term memory in 5 to 7 trials. In contrast, we have previously shown that for simple distractor 380 distributions (such as Gaussian or uniform) one or two trials are enough for observers to develop 381 a probabilistic representation of distractors (Chetverikov et al., 2017b). Representations of more 382 complex distractor distributions take more time (or trials) to develop, but they also progressively 383 change with more repetitions: after one or two trials, bimodal distributions are represented as 384 unimodal, and are only later transformed into bimodal ones. This indicates that more time (trials) 385 is required for sharpening the representation, not for the transfer to long-term memory. 386 A question of how the probabilistic templates for rejection are stored also taps into a 387 more general question, regarding how working memory templates are stored. Recently, 388 Christophel, Iamschinina and colleagues (2018) demonstrated that while attended stimuli in 389 visual working memory are represented both in parietal and frontal cortex in addition to visual

390 cortex, the latter is not involved in representation of unattended stimuli. It is possible that

rejection templates similarly do not involve early visual areas. However, unlike simple

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unattended items, templates for rejection are actively used by observers to guide attention. As
such, their representation might require a level of precision only achievable with the recruitment
of sensory areas.

Won and Geng (Won & Geng, 2018) suggested that distractor templates might be more broadly tuned than target templates. This would allow easy generalization of suppression to similar distractors, while for targets such generalization might be harmful as it would lead to an

398 increased number of false alarms. However, the exact costs of generalization for both target and 399 distractor templates depend on the environment. Specific templates are necessary when a target 400 is similar to distractors, but generalization is helpful otherwise. This has indeed been observed by 401 Geng, DiQuattro, and Helm (Geng, DiQuattro, & Helm, 2017): when a target is similar to 402 distractors, its template is sharpened and shifted away from distractors. Moreover, in the real 403 environment we rarely know how exactly the target or distractors would look under a given 404 illumination and point of view, making some degree of generalization essential for efficient 405 search. In contrast, a typical visual search study would require a very narrow distribution of 406 target features, making a narrow template useful. Our results suggest that distractor templates are 407 specific enough to account for bimodality in the distractor distribution. It remains to be studied whether targets or distractors templates are more specific when their physical distributions are 408 409 equally shaped.

In contrast to our previous studies (Chetverikov et al., 2016, 2017b, 2017d, 2017c), here, we "probed" the distractor representation only at three different points in the feature space. By using targets with a range of features that covered the full feature space, our previous research showed that observers encode the probability distribution of distractors. Here we extend these findings by showing that observers learn the distribution of distractors following a single learning streak. This demonstrates that the previously obtained results are not an artefact of aggregation over multiple trials but rather a true reflection of the templates' content.

We should note that one might interpret our results as simply demonstrating that humans are capable of learning a nonlinear classification rule/decision boundary over a disjoint set in feature space, and can use this to guide visual search. But we think that this alternative proposal is unlikely to hold water because for a simple classifier in this task, learning is not necessary.

421 There is enough information on each trial to easily tell the target from distractors. Moreover, to 422 include learning in the algorithm, learning of the target would suffice, as the target distribution is 423 constant within the learning streak. The fact that our observers struggle with this shows that they 424 do more than strictly necessary. Second, and perhaps more importantly, we showed in our 425 previous work that observers learn the generative model of the data distribution on average 426 rather than learning a simple decision rule (Chetverikov et al., 2016, 2017b, 2017d, 2017c). A 427 decision rule model cannot explain why the response time curves reflect distractor probability 428 both within and outside the distractor distribution range. What determines whether our results 429 support a strong version of the probabilistic templates model, is whether observers learn the 430 distractor distribution on each single learning streak. The aim with the double-target search was 431 to test this specifically.

432

Conclusions

433 We found that rejection templates are probabilistic, similarly to items in visual working 434 memory that receive attention (Ma et al., 2014). However, our study also shows that a template 435 for rejection does not need to be a simple bell-shaped curve, as it is typically modelled in 436 working memory studies. In contrast, their representations are dynamically adapted to task 437 requirements, reflecting the probabilistic nature of the input. Whether such flexibility also 438 characterizes templates for attended items remains to be seen. However, our results clearly 439 demonstrate that probabilistic computations start in the brain even before something is perceived, 440 to determine what should be prioritized in perception.

441 Acknowledgments

- 442 Supported by a grant from the Icelandic Research Fund (IRF #173947-052). AC was supported
- 443 by the Radboud Excellence Initiative. We are grateful to Alena Begler for help with data

444 collection.

445 **Author Contributions**

- 446 All authors participated equally in conceiving and planning the experiments. AC wrote the
- 447 experimental scripts, oversaw the data collection, analyzed the results, and wrote the initial
- 448 version of the manuscript. GC and AK took part in data analyses and interpretation and revised
- the manuscript.
- 450

451	References
452	Alvarez, G. A. (2011). Representing multiple objects as an ensemble enhances visual cognition.
453	Trends in Cognitive Sciences, 15(3), 122–131. https://doi.org/10.1016/j.tics.2011.01.003
454	Arita, J. T., Carlisle, N. B., & Woodman, G. F. (2012). Templates for rejection: Configuring
455	attention to ignore task-irrelevant features. Journal of Experimental Psychology: Human
456	Perception and Performance, 38(3), 580-584. https://doi.org/10.1037/a0027885
457	Bays, P. M. (2015). Spikes not slots: Noise in neural populations limits working memory. Trends
458	in Cognitive Sciences, 19(8), 431-438. https://doi.org/10.1016/j.tics.2015.06.004
459	Bejjanki, V. R., Beck, J. M., Lu, ZL., & Pouget, A. (2011). Perceptual learning as improved
460	probabilistic inference in early sensory areas. Nature Publishing Group, 14(5), 642-648.
461	https://doi.org/10.1038/nn.2796
462	Breiman, L. (1996). Bagging predictors. Machine Learning, 24(2), 123-140.
463	https://doi.org/10.1007/BF00058655
464	Bundesen, C. (1990). A theory of visual attention. Psychol Rev, 97(4), 523-547.
465	https://doi.org/10.1037/0033-295X.97.4.523
466	Chetverikov, A., Campana, G., & Kristjánsson, Á. (2016). Building ensemble representations:
467	How the shape of preceding distractor distributions affects visual search. Cognition, 153,
468	196-210. https://doi.org/10.1016/j.cognition.2016.04.018
469	Chetverikov, A., Campana, G., & Kristjánsson, Á. (2017a). Learning features in a complex and
470	changing environment: A distribution-based framework for visual attention and vision in
471	general. In Progress in Brain Research (Vol. 236, pp. 97–120). Elsevier.
472	https://doi.org/10.1016/bs.pbr.2017.07.001

473 Chetverikov, A., Campana, G., & Kristjánsson, Á. (2017b). Rapid learning of visual ensembles.

- 474 *Journal of Vision*, 17(21), 1–15. https://doi.org/10.1167/17.2.21
- 475 Chetverikov, A., Campana, G., & Kristjánsson, Á. (2017c). Representing Color Ensembles.
- 476 *Psychological Science*, 28(10), 1–8. https://doi.org/10.1177/0956797617713787
- 477 Chetverikov, A., Campana, G., & Kristjánsson, Á. (2017d). Set size manipulations reveal the
- 478 boundary conditions of distractor distribution learning. Vision Research, 140(April), 144–
- 479 156. https://doi.org/10.1016/j.visres.2017.08.003
- 480 Chetverikov, A., Hansmann-Roth, S., Tanrikulu, Ö. D., & Kristjansson, Á. (2019). Feature
- 481 Distribution Learning (FDL): A New Method for Studying Visual Ensembles Perception
- 482 with Priming of Attention Shifts. In *Neuromethods* (pp. 1–21). Springer.
- 483 https://doi.org/10.1007/7657_2019_20
- 484 Christophel, T. B., Iamshchinina, P., Yan, C., Allefeld, C., & Haynes, J. D. (2018). Cortical
- 485 specialization for attended versus unattended working memory. *Nature Neuroscience*,
- 486 21(4), 494–496. https://doi.org/10.1038/s41593-018-0094-4
- 487 Feldman, J. (2014). Probabilistic models of perceptual features. In J. Wagemans (Ed.), Oxford
- 488 *Handbook of Perceptual Organization* (pp. 933–947).
- 489 https://doi.org/10.1093/oxfordhb/9780199686858.013.049
- 490 Geng, J. J., DiQuattro, N. E., & Helm, J. (2017). Distractor probability changes the shape of the
- 491 attentional template. Journal of Experimental Psychology: Human Perception and
- 492 *Performance*, *43*(12), 1993–2007. https://doi.org/10.1037/xhp0000430
- 493 Girshick, A. R., Landy, M. S., & Simoncelli, E. P. (2011). Cardinal rules: visual orientation
- 494 perception reflects knowledge of environmental statistics. *Nature Neuroscience*, 14(7), 926–
- 495 932. https://doi.org/10.1038/nn.2831
- 496 Grubert, A., & Eimer, M. (2013). Qualitative differences in the guidance of attention during

- 497 single-color and multiple-color visual search: Behavioral and electrophysiological evidence.
- 498 Journal of Experimental Psychology: Human Perception and Performance, 39(5), 1433–
- 499 1442. https://doi.org/10.1037/a0031046
- 500 Kersten, D., Mamassian, P., & Yuille, A. (2004). Object Perception as Bayesian Inference.
- 501 Annual Review of Psychology, 55(1), 271–304.
- 502 https://doi.org/10.1146/annurev.psych.55.090902.142005
- 503 Kristjánsson, Á., & Driver, J. (2008). Priming in visual search: separating the effects of target
- 504 repetition, distractor repetition and role-reversal. *Vision Research*, 48(10), 1217–1232.
- 505 https://doi.org/10.1016/j.visres.2008.02.007
- 506 Lamy, D. F., Antebi, C., Aviani, N., & Carmel, T. (2008). Priming of Pop-out provides reliable
- 507 measures of target activation and distractor inhibition in selective attention. *Vision*
- 508 *Research*, 48(1), 30–41. https://doi.org/10.1016/j.visres.2007.10.009
- 509 Ma, W. J. (2012). Organizing probabilistic models of perception. *Trends in Cognitive Sciences*,
- 510 *16*(10), 511–518. https://doi.org/10.1016/j.tics.2012.08.010
- 511 Ma, W. J., Husain, M., & Bays, P. M. (2014). Changing concepts of working memory. *Nature*
- 512 *Neuroscience*, *17*(3), 347–356. https://doi.org/10.1038/nn.3655
- 513 Ma, W. J., Navalpakkam, V., Beck, J. M., van den Berg, R., & Pouget, A. (2011). Behavior and
- 514 neural basis of near-optimal visual search. *Nature Neuroscience*, *14*(6), 783–790.
- 515 https://doi.org/10.1038/nn.2814
- 516 Ma, W. J., Shen, S., Dziugaite, G., & van den Berg, R. (2015). Requiem for the max rule? Vision
- 517 *Research*, *116*, 179–193. https://doi.org/10.1016/j.visres.2014.12.019
- 518 Maljkovic, V., & Nakayama, K. (1994). Priming of pop-out: I. Role of features. Memory &
- 519 *Cognition*, 22(6), 657–672. Retrieved from http://www.ncbi.nlm.nih.gov/pubmed/7808275

- 520 Oberauer, K. (2002). Access to Information in Working Memory: Exploring the Focus of
- 521 Attention. Journal of Experimental Psychology: Learning Memory and Cognition, 28(3),
- 522 411–421. https://doi.org/10.1037//0278-7393.28.3.411
- 523 Olivers, C. N. L., Peters, J., Houtkamp, R., & Roelfsema, P. R. (2011). Different states in visual
- 524 working memory: When it guides attention and when it does not. *Trends in Cognitive*
- 525 *Sciences*, *15*(7), 327–334. https://doi.org/10.1016/j.tics.2011.05.004
- 526 Peirce, J. W. (2007). PsychoPy--Psychophysics software in Python. Journal of Neuroscience

527 *Methods*, *162*(1–2), 8–13. https://doi.org/10.1016/j.jneumeth.2006.11.017

- 528 Peirce, J. W. (2009). Generating stimuli for neuroscience using PsychoPy. Frontiers in
- 529 *Neuroinformatics*, 2. https://doi.org/10.3389/neuro.11.010.2008
- 530 Rao, R. P., Olshausen, B. A., & Lewicki, M. S. (2002). *Probabilistic models of the brain:*
- 531 *Perception and neural function.* MIT Press.
- van Moorselaar, D., Theeuwes, J., & Olivers, C. N. L. (2014). In competition for the attentional
- 533 template: Can multiple items within visual working memory guide attention? *Journal of*
- 534 *Experimental Psychology: Human Perception and Performance*, 40(4), 1450–1464.
- 535 https://doi.org/10.1037/a0036229
- 536 Vickery, T. J., King, L.-W., & Jiang, Y. (2005). Setting up the target template in visual search.
- 537 *Journal of Vision*, 5(1), 8. https://doi.org/10.1167/5.1.8
- 538 Wang, D., Kristjánsson, Á., & Nakayama, K. (2005). Efficient visual search without top-down or
- 539 bottom-up guidance. *Perception & Psychophysics*, 67(2), 239–253.
- 540 https://doi.org/10.3758/BF03206488
- 541 Won, B.-Y. Y., & Geng, J. J. (2018). Learned suppression for multiple distractors in visual
- search. Journal of Experimental Psychology: Human Perception and Performance, 44(7),

- 543 1128–1141. https://doi.org/10.1037/xhp0000521
- 544 Woodman, G. F., Carlisle, N. B., & Reinhart, R. M. G. (2013). Where do we store the memory
- 545 representations that guide attention? *Journal of Vision*, *13*(3), 1–1.
- 546 https://doi.org/10.1167/13.3.1

547

Supplemental experiment

550 Method

551	Participants. Fifteen observers (ten female, age $M = 25.47$) at St. Petersburg State
552	University, Russia, took part in a single experimental session lasting approximately 30 min. Two
553	of them were excluded because their response times were very high compared with the other
554	observers (1356 and 1393 ms for excluded observers vs. 761 ms for the remaining sample). One
555	more was excluded because of low accuracy ($M = 0.71$ vs. 0.83 for the remaining sample). The
556	study was approved by the ethics committee of St. Petersburg State University.
557	Procedure. We used a task similar to our previous studies (Chetverikov et al., 2016,
558	2017b). Stimuli were presented on an Acer V193 display (19" with 1280×1024 pixel resolution)
559	using PsychoPy 1.84.2 (Peirce, 2007, 2009). Viewing distance was ~ 60 cm. Observers searched
560	for an oddly oriented line in a 6×6 grid of 36 lines subtending $16^{\circ} \times 16^{\circ}$ at the centre of a display.
561	The length of each line was 1.41°. Line positions were jittered by randomly adding a value
562	between $\pm 0.5^{\circ}$ to both vertical and horizontal coordinates. Observers indicated whether the target
563	line was in the upper or the lower half of the screen by pressing the 'i' or 'j' keys on a standard
564	keyboard. Trials were organized in intertwined prime and test 'streaks'. During prime streaks,
565	distractors were randomly drawn from a bimodal distribution that included two uniform parts
566	with orientations ranging from -40 to -20 and +20 to +40 relative to the overall mean. The
567	distribution mean was the same within streak but chosen randomly between streaks. Target
568	orientation was selected randomly on each trial with the restriction that the distance between
569	target orientation and distractor mean in feature space was 60 degrees at minimum. Based on the

570	results of previous studies, prime streak length was set to 6-7 trials because this streak length is
571	sufficient to encode bimodal distributions with relative accuracy (Chetverikov et al., 2017b).
572	Within test streaks, distractor orientations were randomly drawn from a truncated
573	Gaussian with $SD = 10$ deg. and range 20 deg. Each test streak had two trials and the targets on
574	these trials (target type) were either located on the "peaks" of the previous bimodal distribution
575	(within the +/- 25 to 35 deg. range relative to the previous distractors' mean), in-between the
576	peaks (within 0 to +/-5 deg. range) or outside the previous distribution range (within +/- 55 to 90 \pm
577	deg. range). Three types of test streaks were used with targets on the first and the second test trial
578	either on two different peaks, on a peak and in-between the peaks, or on a peak and outside the
579	previous distribution range. These three conditions were presented equally often in random
580	order. The order of targets within the test trials for each condition was counterbalanced. The
581	distractor mean was chosen randomly with a distance to the target of no less than 60 deg (as on

582 prime trials).

Observers participated in one session of approximately 1244 trials divided into 288 prime and test streaks. Decision time was not limited but participants were encouraged to respond as quickly and accurately as possible. Feedback based on search time and accuracy on previous trials was presented after each trial was shown in the upper-left corner of the screen to motivate participants. The current trial number and the total number of trials were shown beneath the score. If observers made an error, the word "ERROR" appeared in red letters at display centre for 1 second.

590 Results

591	Overall performance. Participants were slower ($M = 738$ [683, 794] vs. $M = 615$ [589,
592	643], $t(11.0) = 5.67$, $p < .001$, $d = 1.64$) and less accurate ($M = 0.78$ [0.75, 0.82] vs. $M = 0.96$
593	[0.95, 0.97], t(11.0) = -10.29, p < .001, d = 2.97) on learning trials than test trials, due to the fact
594	that learning trials had a broader distribution. Response times decreased while accuracy
595	increased during learning trials: A linear mixed-effects regression indicated that the first trials in
596	each learning sequence were slower, ($B = 0.08$, $SE = 0.02$, $t(11.47) = 4.52$, $p < .001$) and less
597	accurate ($B = -0.04$, $SE = 0.01$, $t(12.52) = -4.50$, $p < .001$) than the later trials.
598	Test trials. On test trials, observers' performance depended on both target type and
599	condition. Replicating the results of Chetverikov et al. (2017b), on the first trial in a test
600	sequence observers responded more slowly when the target was at one of the peaks of the
601	preceding distractor distribution than when it was in-between the peaks ($t(11.0) = 3.94$, $p = .002$,
602	d = 1.14), while responses for the in-between the peaks targets were slower than when they were
603	outside the range of the previous distribution ($t(11.0) = 3.96$, $p = .002$, $d = 1.14$).